

On the Stability of a Family of Matrix Polynomials

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Abstract.

This talk investigates the stability of a specific class of matrix polynomials with complex coefficients. Namely, we consider a family of matrix polynomials of the form

$$\mathbf{f}_n(z) = \mathbf{A}_0 z^n + \mathbf{A}_1 z^{n-1} + \dots + \mathbf{A}_n,$$

where each coefficient \mathbf{A}_j is a $q \times q$ complex matrix. Using the Hermite-Biehler-type decomposition

$$\mathbf{f}_n(z) = \mathbf{h}_n(z^2) + z\mathbf{g}_n(z^2),$$

together with the theory of Bezoutian forms and orthogonal matrix polynomials on the interval $[0, +\infty)$, we prove that $\mathbf{f}_n(z)$ is a stable matrix polynomial. Specifically, we demonstrate that the determinantal polynomial $\det \mathbf{f}_n(z)$ has all its roots situated in the open left-half of the complex plane \mathbb{C} . These results provide a deeper link between the theory of orthogonal matrix polynomials and the robust stability of multi-variable dynamical systems.